DEPARTMENT OF MATHEMATICS

Ph.D (Mathematics) ACADEMIC SESSION 2010 onwards



J.C. BOSE UNIVERSITY OF SCIENCE AND TECHNOLOGY, YMCA

J. C. BOSE UNIVERSITY OF SCIENCE AND TECHNOLOGY, YMCA FARIDABAD DEPARTMENT OF MATHEMATICS

Subject	Title	L	Т	Р	Sessional	Final	Total	Credits	Category
code					Marks	Exam			Code
						Marks			
PHAS- 06	Operation Research	4	0	0	40	60	100	4	DCC
PHAS- 07	Fixed Point Theory	4	0	0	40	60	100	4	DCC
PhD- 100A	Research Methodology	4	0	0	40	60	100	4	DCC

SCHEME OF Ph.D MATHEMATICS(Course Work)(2010)

SCHEME OF Ph.D MATHEMATICS(Course Work)(2016)

Subject code	Title	L	Т	Р	Sessional Marks	Final Exam Marks	Total	Credits	Category Code
PHAS-	Reliability Theory and	4	0	0	40	60	100	4	DCC
09	its Application								
PhD-	Research	4	0	0	40	60	100	4	DCC
100A	Methodology								

SCHEME OF Ph.D MATHEMATICS(Course Work)(2018)

Subject code	Title	L	Т	Р	Sessional Marks	Final Exam Marks	Total	Credits	Category Code
PHDM- 01	Operation Research	4	0	0	25	75	100	4	DCC
PhD- 100A	Research Methodology	4	0	0	25	75	100	4	DCC

Syllabus of Operations Research for Ph.D Coursework

Code: PHAS-06

UNIT 1: Linear Programming Problem:

- (i) Computational procedure of simplex method
- (ii) Alternative optimum solutions: unbounded solutions, non-existing feasible solutions.
- (iii) Big M method, Two phase method
- (iv) Sensitivity Analysis
- (v) Revised Simplex Method
- (vi) Duality, Dual Simplex Method
- UNIT 2: Inventory Models
 - (i) Various costs
 - (ii) Deterministic inventory models
 - (iii) Single period inventory model with shortest cost
 - (iv) Stochastic models
 - (v) Application of inventory models
 - (vi) Economic lot sizes-price breaks
- UNIT 3: Queuing theory
 - (i) Introduction to Queues
 - (ii) Basic Elements of Queuing Models
 - (iii) Queue Disciplines
 - (iv) Role of Exponential and Poisson Distributions
 - (v) Markovian Process, Erlang Distribution
 - (vi) Distribution Of Arrivals, Distribution of Service Times
 - (vii) Definition of Steady and Transient State, Poisson Queues.
- UNIT 4: Integer linear programming
 - (i) Integer Linear Programming Problems
 - (ii) Mixed Integer Linear Programming Problems
 - (iii) Cutting Plane Method
 - (iv) Branch and Bound Method
 - (v) 0-1 integer linear programming problem.

UNIT 5: Non linear programming & Quadratic programming

- (i) Formulation of non linear programming problems
- (ii) General non linear programming
- (iii) Canonical form of non linear programming problem
- (iv) Kuhn Tucker conditions, non negative constraints
- (v) General quadratic programming problem
- (vi) Wolfe's modified simplex method

(vii) Beale's method

UNIT 6: <u>Dynamic Programming</u>

- (i) Bellman's Principle of optimality of Dynamic Programming
- (ii) Multistage decision problem and its solution
- (iii) Solution of linear programming problems as a Dynamic Programming Problem

<u>Books</u>

- Hadley, G.,"Linear Programming, and Massachusetts", Addison-Wesley
- Taha, H.A, "Operations Research An Introduction", Macmillian
- Hiller, F.S., G.J. Lieberman, "Introduction to Operations Research", Holden-Day
- Harvey M. Wagner, "Principles of Operations Rsearch with Applications to Managerial Decisions", Prentice Hall of India Pvt. Ltd.
- Swarup K., "Operations Research", S. Chand

Syllabus for Pre-Ph.D. Programme

Fixed Point Theory

Section-I

Metric spaces and topological spaces, neighbourhoods, limit points, open and closed sets, completeness of metric spaces, Cantor's intersection theorem, contraction mappings, contraction principle and its converse, continuous and uniform continuous functions in metric spaces, compact metric spaces.

Section-II

Normed linear spaces, Banach spaces, fixed points, Lipschitz, non-expansive, contractive, contraction mappings and relation between these mappings, retraction mapping, \in - chain and \in - chainable metric spaces. Brouwers and Schauder's fixed point theorems and applications.

Section-III

Probabilistic metric spaces, Fuzzy Metric Spaces, Intuitionistic fuzzy metric Spaces, Various types of mappings such as commuting mappings, compatible mappings and their variants.

Suggested books:

- 1. Istratescu, V.I., Fixed Point Theory: An Introduction, Springer.
- 2. Joshi, M.C. and Bose, R.K., Some Topics in Non-Linear Functional Analysis, John Wiley

& Sons (Asia).

3. J. Dugundji and A. Granas, Fixed Point Theory, Springer.

4. Agarwal, R.P., Meehan, M., and O' Regan, D., Fixed Point Theory and Applications, Cambridge Tracts in Mathematics, 141, Cambridge University Press.

Ph.D Coursework

Reliability Theory And its Application (PHM-101)

No. of Credits: 4	Sessional: 40 Marks
LTP Total	Theory : 60 Marks
400 4	Total : 100 Marks
	Duration of Exam: 3 Hours

Part-A

Probability generating function: Probability generating function (pgf) of Bernoulli, binomial, Poisson and geometric distributions, Mean and variance of probability distributions using pgf. Mean and variance of probability distributions in terms of Laplace transforms. Stochastic Processes: definition, classification and examples. Markov Chains: definition and examples, transition matrix, order of a Markov chain, Markov chain as graphs.

Part-B

Reliability and Quality. Failure Data Analysis: Failure data, Failure density, Failure rate. Some Important distributions: Exponential, Rayleigh, Weibul, Gamma and Lognormal distributions.

Laplace and Stieltjes transforms and convolutions.

Component Reliability and Hazard Models: Component reliability from test data, Mean time to failure (MTTF), Mean time between failures (MTBF), Time dependent hazard models. Bath-Tub Curve.

Part-C

System Reliability Models: Systems with components in series, Systems with parallel components, k-out-of-m systems, Non-series parallel systems, Systems with mixed mode failures. Standby redundancy: Simple standby system, k-out-of-n standby system.

Part-D

Maintainability and Availability: Maintainability function, Availability function, Reliability and availability analysis of a two-unit parallel system with repair using Markov model, Reliability and availability analysis of single-unit and two- unit cold standby systems with constant failure and repair rates using regenerative point and supplementary variable techniques.

Economics of Reliability Engineering: Manufacture's cost, Customer's cost, Reliability achievement and utility cost models, Depreciation cost models and availability cost model for parallel system.

Books Recommended:

1. E. Balagurusami, Reliability Engineering, Tata McGraw Hill, New Delhi, 1984.

2. L. S. Srinath, Reliability Engineering, Affiliated East West Press, New Delhi, 1991.

3. Elsayed A. Elsayed, Reliability Engineering, Addison Wesley Longman. Inc. Publication

4. A. Birolini, Reliability Engineering: Theory and Practical, Springer-Verlag.

5. Jai Singh Gurjar, Reliability Technology, I.K. International Publishing House Pvt. Ltd

6. Charles E Ebeling, An Introduction to Reliability and Maintainability Engineering, Tata McGraw-Hill Publishing Company Limited, New Delhi,2000

Ph.D Coursework Operations Research Code: PHDM-01 No of Credits: 4

		Sessional:	25
L	Р	Theory Exam:	75
4	0	Total:	100

UNIT 1

Linear Programming Problem: Computational procedure of simplex method, Alternative optimum solutions: unbounded solutions, non-existing feasible solutions. Big M method, Two phase method, Sensitivity Analysis, Revised Simplex Method, Duality, Dual Simplex Method.

UNIT 2

Inventory Models: Various costs, Deterministic inventory models, Single period inventory model with shortest cost, Stochastic models, Application of inventory models, Economic lot sizes-price breaks.

UNIT 3

Assignment problem, mathematical formulation, solution of assignment problem (Hungarian method), Transportation problem, mathematical formulation. Initial basic feasible solution of transportation problem by North-west corner rule, Lowest-cost Entry method and Vogel's approximation method, Optimal solution of transportation problem.

UNIT 4

Integer linear programming: Integer Linear Programming Problems, Mixed Integer Linear Programming Problems, Cutting Plane Method, Branch and Bound Method.

Queuing theory: Introduction to Queues, Basic Elements of Queuing Models, Queue Disciplines, Role of Exponential and Poisson Distributions, Markovian Process, Erlang Distribution, Distribution of Arrivals, Distribution of Service Times, Definition of Steady and Transient State, Poisson Queues.

Books:

- Hadley, G., "Linear Programming, and Massachusetts", Addison-Wesley
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- Swarup K., "Operations Research", S. Chand

PHD - 100A

RESEARCH METHODOLOGY PhD (Common Subject)

No. of Credits: 4	Sessional:	25 Marks
L T P Total	Theory:	75 Marks
4 0 0 4	Total:	100 Marks
	Duration of Exam:	3 Hours

Course Objectives:

Understand research process in order to plan a research proposal

Learn methods to devise and design a research set-up

Plan and perform data collection methods and its analysis

Conclude research in report writing

Course Outcomes: The research scholar shall be able to

CO1 Plan a research proposal and design the research.

CO2 Collect data through experiments or surveys as per research requirement. CO3 Understand and apply sampling and sampling distributions.

CO4 Understand and perform quantitative and qualitative data analysis. CO5 Write research report with proper citations.

- *Unit 1* Introduction to Research: Definition, need and purpose of research, types of research, research process, approaches to research, planning a research proposal, literature review.
- Unit 2 Measurement Scales: Indexes vs. Scales, Types of Scale, construction of Scale, Bogardus social distance scale, Thurstone Scale, Likert Scale, Semantic Differential Scale, Guttmann Scale.
- Unit 3 Data Collection Methods: Experiments and Surveys, Experiments: Classical Experiments, Independent & Dependent Variables, Pre Testing & Post Testing, Double Blind Experiment, Subject Selection, Variation on Experiment Design. Survey Research: Topics appropriate for survey research, Guidelines for asking questions, Questionnaire Construction, Strengths & Weakness of Survey Research, Types of Surveys.
- Unit 4 Sampling: Types of sampling methods: Non Probability Sampling, Probability Sampling, Theory & Logic of Probability Sampling, Sampling Distributions & Estimates of Sampling Error.
- Unit 5 Data Analysis: Qualitative v/s Quantitative data analysis, Qualitative Data Analysis: Discovering Patterns, Grounded Theory Method, Semiotics, Conversation Analysis, Qualitative Data Processing. Quantitative Data Analysis: Quantification of Data, Univariate Analysis, Bivariate Analysis,

Multivariate Analysis, Regression Analysis, Description Analysis. Hypothesis. Multiple Attribute Decision Making.

Unit 6 Report Writing, Ethical Issues and Outcomes: Report Preparation, Structure of Report, Report Writing Skills, Citations, Research Papers, Intellectual Property Rights, Plagiarism, Patent, Commercialization, Ethical Issues.

References:

1. Research Methodology by R. Panneerselvam, 2nd Ed. PHI

2. Research Methodology by C.R. Kothari & Gaurav Garg, 3rd Ed. New Age Publishers

- 3. Research Methodology and Scientific Writing by C. George Thomas, Ane Books
- 4. The practice of social research by Earl Babbie, 14th Ed. Cengage
- 5. Multiple Attribute Decision Making, Gwo-Hshiung Tzeng and Jih-Jeng Huang, CRC Press

Mapping of the subjects

S.	Course Name	Course Code	Employability	Entrepreneurship	Skill
No.					Development
1.	Operation	PHDM-01	✓	✓	-
	Research				
2.	Research	PhD-100A	\checkmark	-	\checkmark
	Methodology				